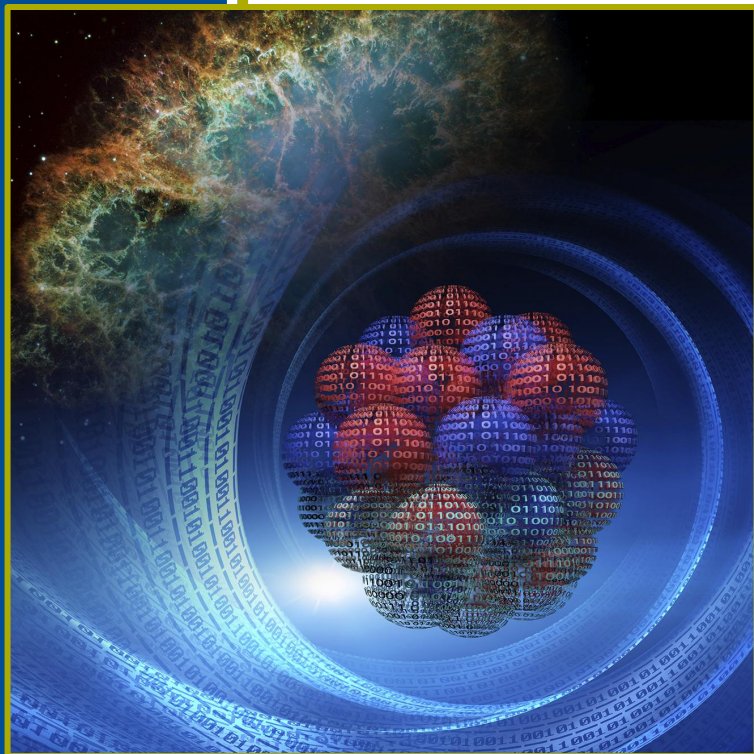




Andy Sproles, ORNL

Symmetry breaking on the scale of the nuclear chart

W. Ryssens, G. Scamps and S. Goriely

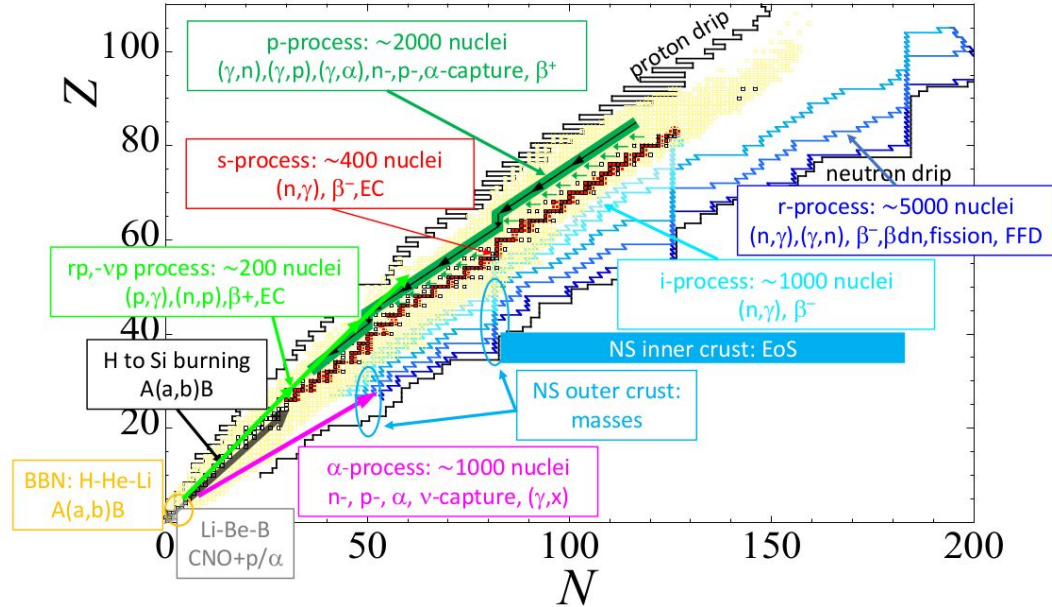
April 21th 2022



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The challenge for nuclear theory



Skyrme **E**nergy **D**ensity **F**unctionals (**EDFs**)

$$E \sim \int d^3r \left[C^\rho \rho(\mathbf{r})\rho(\mathbf{r}) + C^\tau \tau(\mathbf{r})\rho(\mathbf{r}) + \dots \right]$$

Diagram illustrating the Skyrme Energy Density Functional (EDF) formula:

- Energy (to be varied)**: Indicated by a yellow box around E .
- Coupling constants**: Indicated by a blue line connecting the constants C^ρ and C^τ to the text.
- Local densities of a mean-field state**: Indicated by a red line connecting the density terms $\rho(\mathbf{r})\rho(\mathbf{r})$ and $\tau(\mathbf{r})\rho(\mathbf{r})$ to the text.

Strong points

- **Microscopic** approach
- # of **observables** accessible
- Feasible for **1000s** of nuclei

Weak points

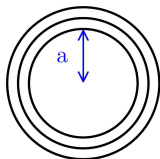
- Simple ansatz
- **Phenomenological** form
- Fitting of **coupling constants**

Brussels models

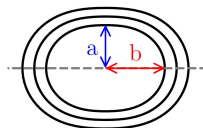
- **20-25** parameters
- grasp physics of the entire chart
- Fit protocol includes:
 - 1000s of masses
 - 100s of charge radii
 - INM properties

Symmetry breaking

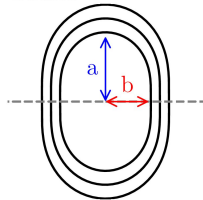
Spherical



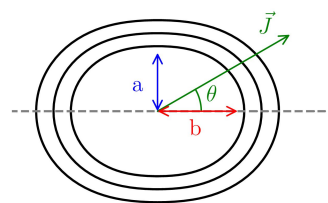
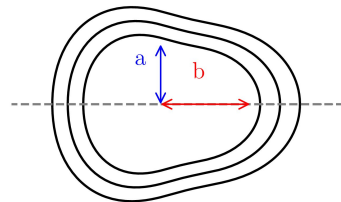
Prolate



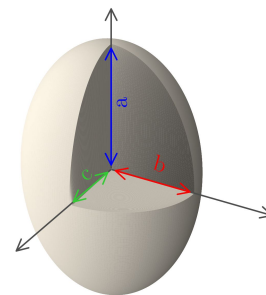
Oblate



One DOF: β_{20}



Two DOF: (β_{20}, β_{22}) or (β, γ)



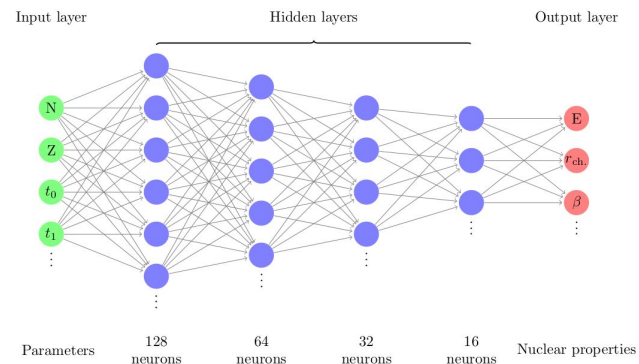
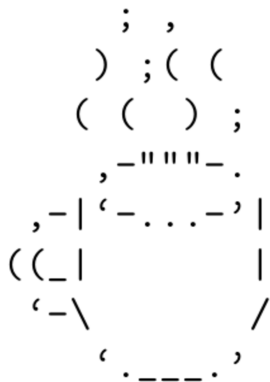
Nuclear deformation

- Cheap way to grasp more **correlations**
- **intuitive interpretation** of results
- State-of-the-art for global models:
 - time-reversal invariance
 - reflection symmetry
 - axial symmetry

Including complicated geometries

- **reflection-asymmetric** shapes
- **time-reversal** breaking
- **cluster** structures
- **triaxial** shapes
-

Tools: MOCCa and machine learning



MOCCa

W. R. PhD Thesis, ULB (2016).
W. R. et al., PRC 92, 064318 (2015).
W. R. et al., EPJA 55, 93 (2019).

- Skyrme-HFB solver in **3D coordinate space**
- Very flexible for **symmetries/shapes**
- High numerical **accuracy**
- New algorithms for **speed** and **robustness**

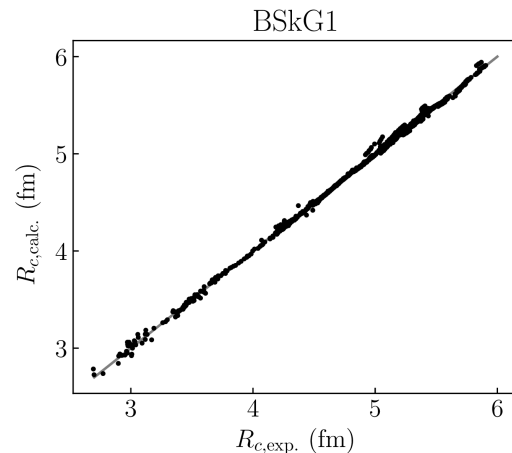
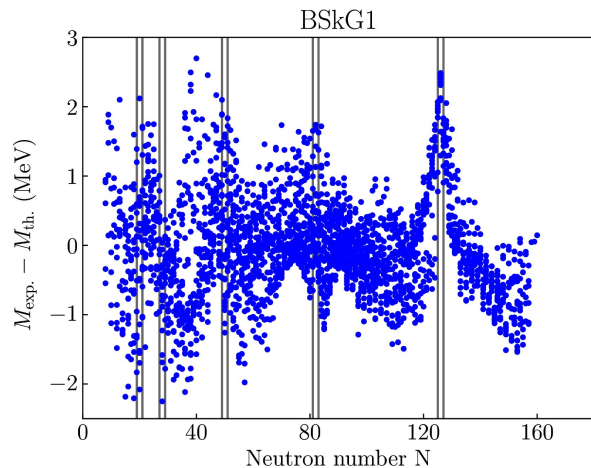
Machine learning

G. Scamps et al., EPJA 57, 333 (2021).

- **100's** of neural networks
- each trained to emulate MOCCa
- exploration of parameter space

There are no ML extrapolations!

Brussels **S**kyrme on a **G**rid: BSkG1 and BSkG2



BSkG1: G. Scamps et al., EPJA 57, 333 (2021).
BSkG2: W. Ryssens et al., in preparation
HFB-21: S. Goriely et al., PRC 82, 035804 (2010).
FRDM: P. Möller et al., At. Data Nucl. Data Tables, 109-110 (2016).

Both models fitted with

- >2400 masses
- >800 charge radii
- triaxial deformation
- high numerical accuracy

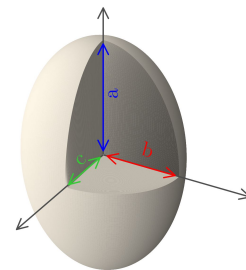
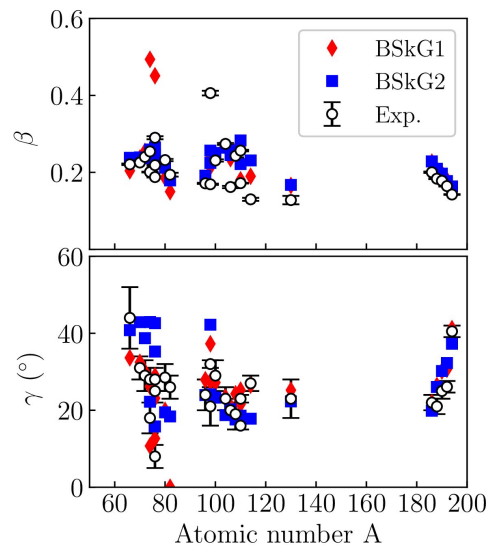
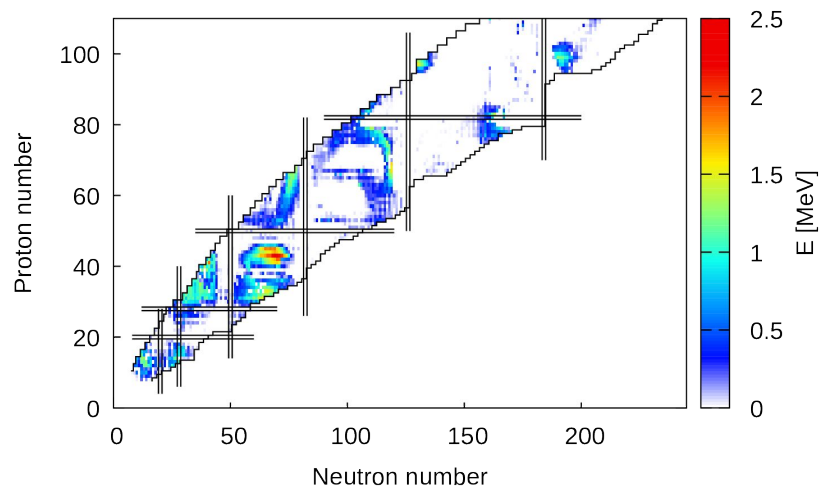
Extra for BSkG2:

- **time-reversal** breaking
- **vibrational** correction
- **12 fission barriers**

Global performance

σ^2	BSkG1	BSkG2	HFB-21	FRDM
Masses (MeV)	0.741	0.678	0.577	0.560
Charge radii (fm)	0.027	0.027	0.027	0.038

Triaxial deformation



Two DOF: (β_{20}, β_{22}) or (β, γ)

Energy gain by triaxial deformation

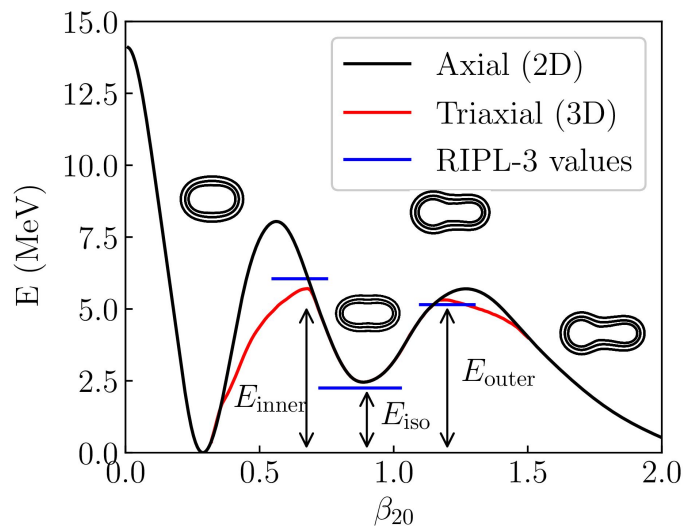
- Many nuclei gain **0.5-2.5 MeV**
- Highest gains for $Z \sim 43$ (Rh)

Rotational invariants

All refs in G. Scamps et al., EPJA 57, 333 (2021).

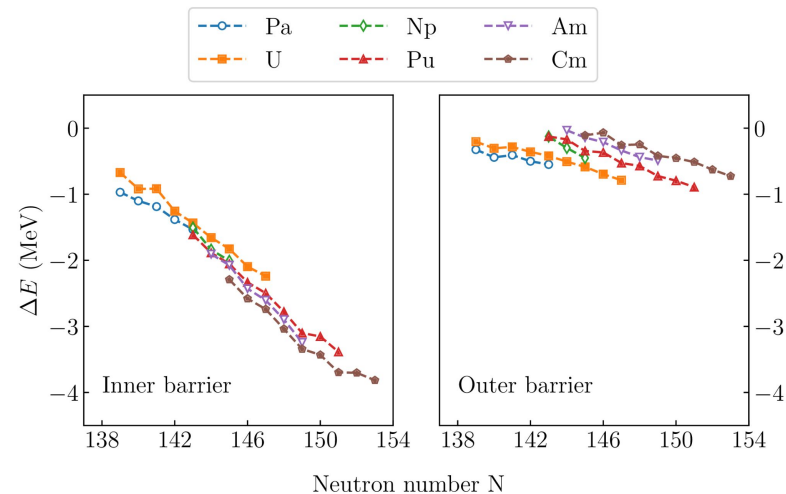
- obtained from COULEX
- data compiled by M. Zielińska

Fission barriers of actinides



Fission barriers with BSkG2

- collective correction parameters (5)
- refit to 12 actinide barriers after mass fit



HFB-14: S. Goriely et al., PRC 75, 064312 (2007).
FRLDM: P. Möller et al., PRC 79, 064304 (2009).

Performance on 41 barriers ($Z > 90$) + 25 isomers

$\sigma^2(\text{MeV})$	BSkG1	BSkG2	HFB-14	FRLDM
Primary barriers	0.87	0.45	0.61	0.79
Secondary barriers	0.86	0.45	0.70	1.35
Isomers	0.45	0.48	0.93	1.04

The BSkGX models

Today's models:

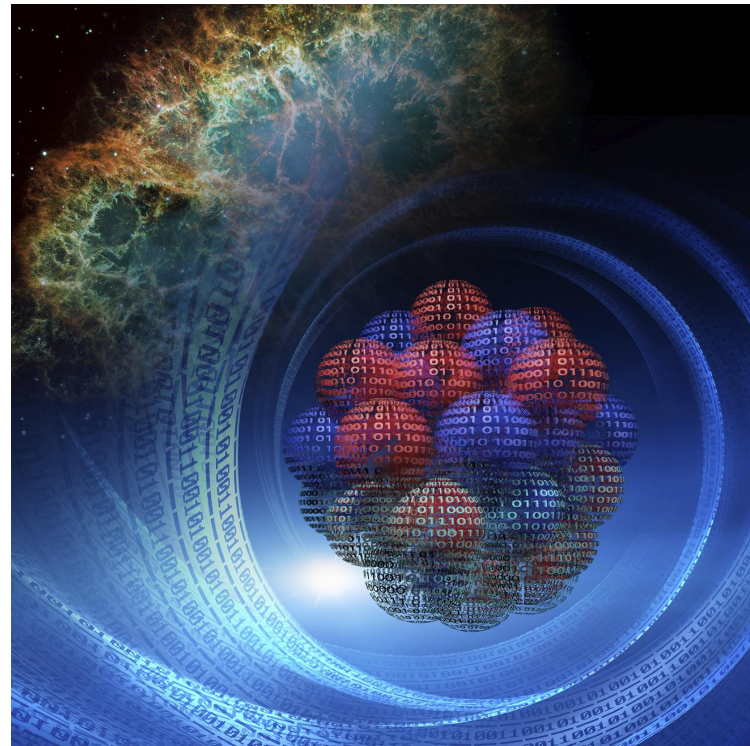
- fitted to > 2400 masses and > 800 radii
- among the best for **masses** and **charge radii**
- include **triaxiality** (BSkG1/2)
- include **time-odd** channel (BSkG2)
- the best for actinide fission barriers (BSkG2)

We are working on constructing:

- nuclear level densities
- complete fission model

Tomorrow's models:

- improved neutron matter equation-of-state
- improved spectroscopy
- octupole deformation



Thank you for...

..... the help!



S. Goriely
G. Grams



M. Bender



G. Scamps

..... the computing time!



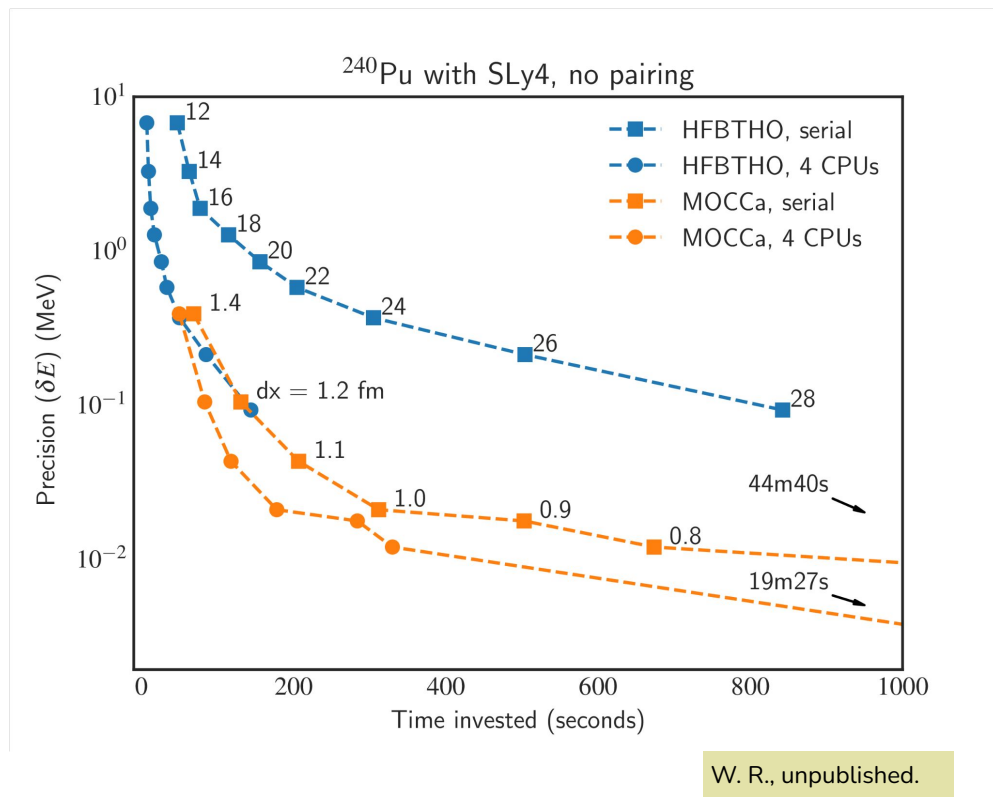
..... the funding!



..... your attention!

Bonus!

MOCCa is **fast** and **accurate**

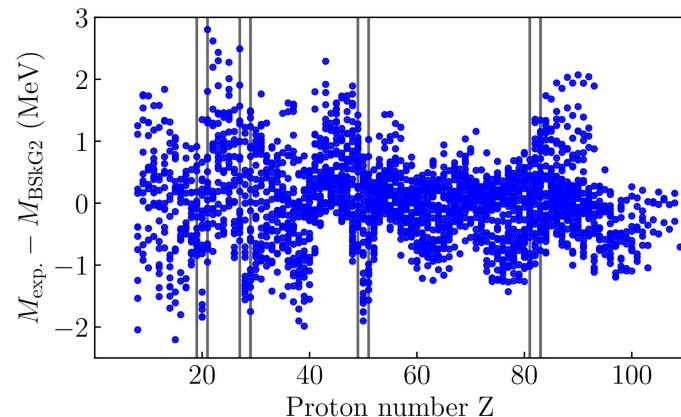
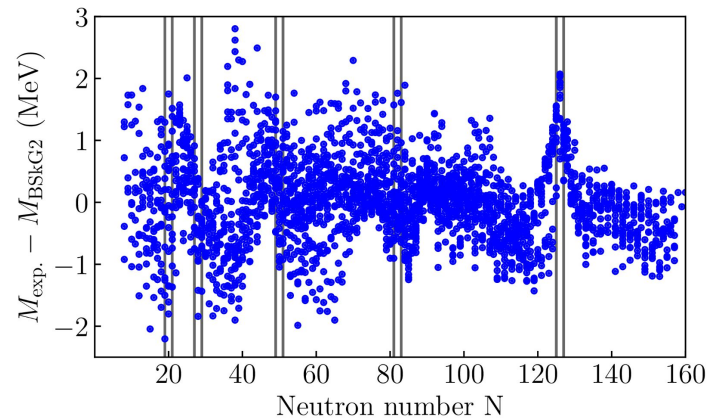


BStG models: details

W. R. et al., in preparation.

Table IV. Rms σ and mean $\bar{\epsilon}$ (exp.-theory) deviations with respect to the 2457 known masses ($Z, N \geq 8$) M [57], the 2309 neutron separation energies S_n , the 2173 β -decay energies Q_β , and the 884 measured charge radii R_c [58] for the BSkG1 and BSkG2 mass models. The first line gives the model error [59] on all the 2457 measured masses. ^a

Results	BSkG1	BSkG2
$\sigma_{\text{mod}}(M)$ [MeV]	0.734	0.668
$\sigma(M)$ [MeV]	0.741	0.678
$\bar{\epsilon}(M)$ [MeV]	-0.026	0.026
$\sigma(S_n)$ [MeV]	0.466	0.500
$\bar{\epsilon}(S_n)$ [MeV]	0.000	-0.006
$\sigma(Q_\beta)$ [MeV]	0.645	0.619
$\bar{\epsilon}(Q_\beta)$ [MeV]	0.000	-0.019
$\sigma(R_c)$ [fm]	0.0267	0.0274
$\bar{\epsilon}(R_c)$ [fm]	-0.0008	-0.007
$\sigma(\Delta R_c)$ [fm]	0.0150	0.0169

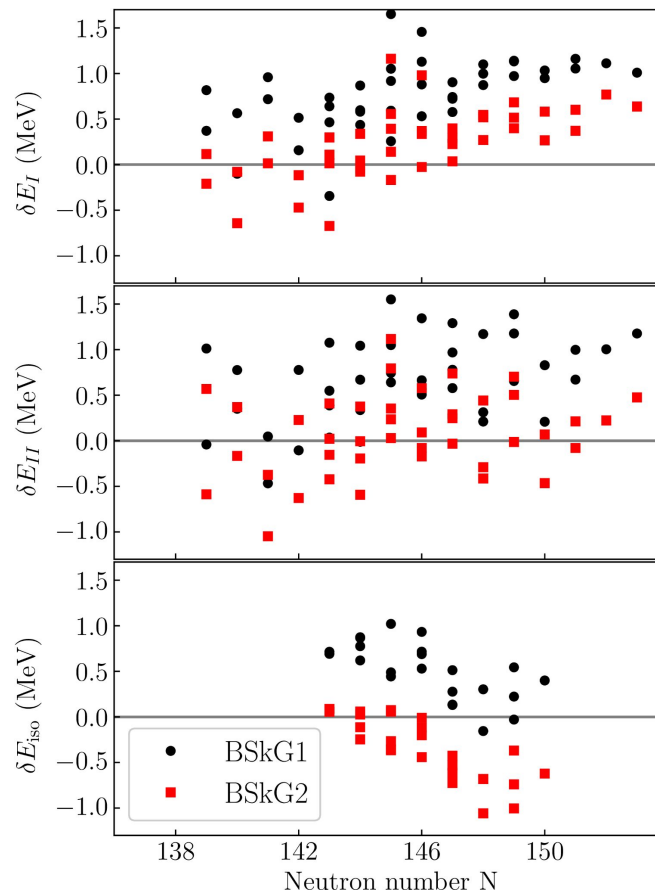


BStG models: fission

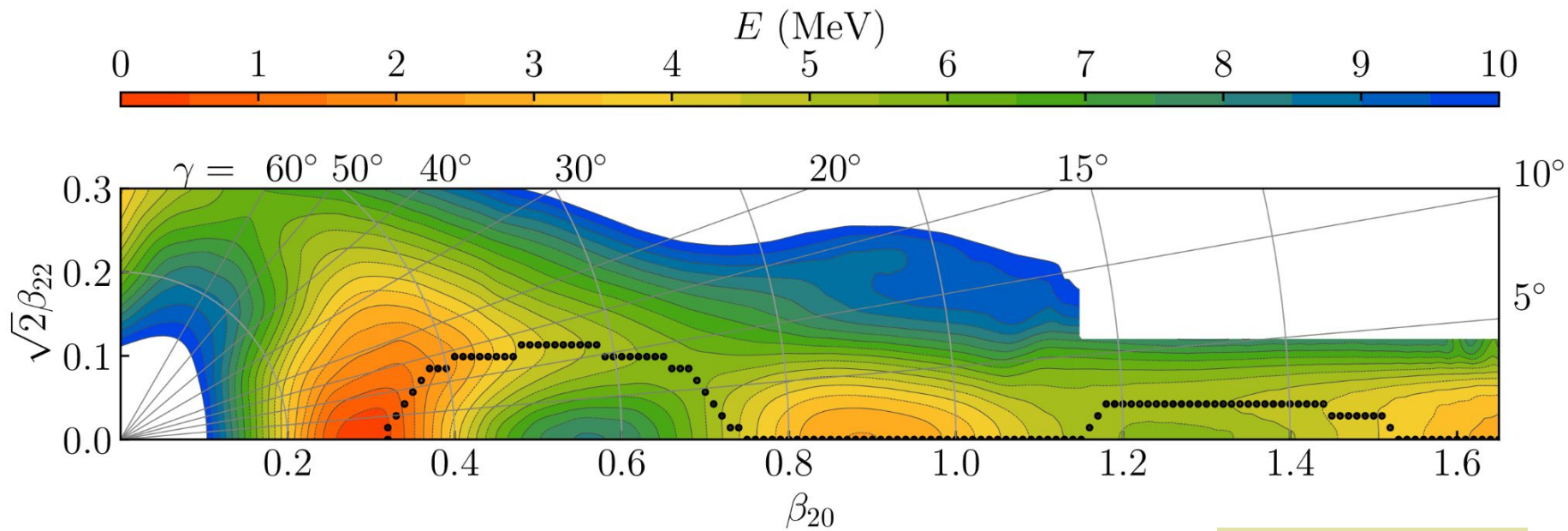
W. R. et al., in preparation.

			BSkG1		BSkG2	
			σ	$\bar{\epsilon}$	σ	$\bar{\epsilon}$
Fit-data	Primary	12	+0.92	+0.88	+0.47	+0.32
	Secondary	12	+0.71	+0.57	+0.38	-0.10
	Isomers	7	+0.67	+0.58	+0.48	-0.32
Even-even	Primary	12	+0.92	+0.88	+0.47	+0.32
	Secondary	12	+0.71	+0.57	+0.38	-0.10
	Isomers	7	+0.67	+0.58	+0.48	-0.32
Other	Primary	29	+0.84	+0.74	+0.45	+0.21
	Secondary	29	+0.91	+0.76	+0.48	+0.16
	Isomers	18	+0.47	+0.77	+0.47	-0.35
Total	Primary	41	+0.87	+0.78	+0.45	+0.24
	Secondary	41	+0.86	+0.70	+0.45	+0.08
	Isomers	25	+0.45	+0.77	+0.48	-0.34

Table VI. Rms deviations σ_X and mean deviations $\bar{\epsilon}_X$ between RIPL-3 [29] and BStG1 and BStG2 calculated values for the primary and secondary barrier heights (data for 41 nuclei with for $90 < Z \leq 96$), as well as isomer excitation energies from Ref. [30] (data for 25 nuclei with for $90 < Z \leq 96$). All quantities in MeV.

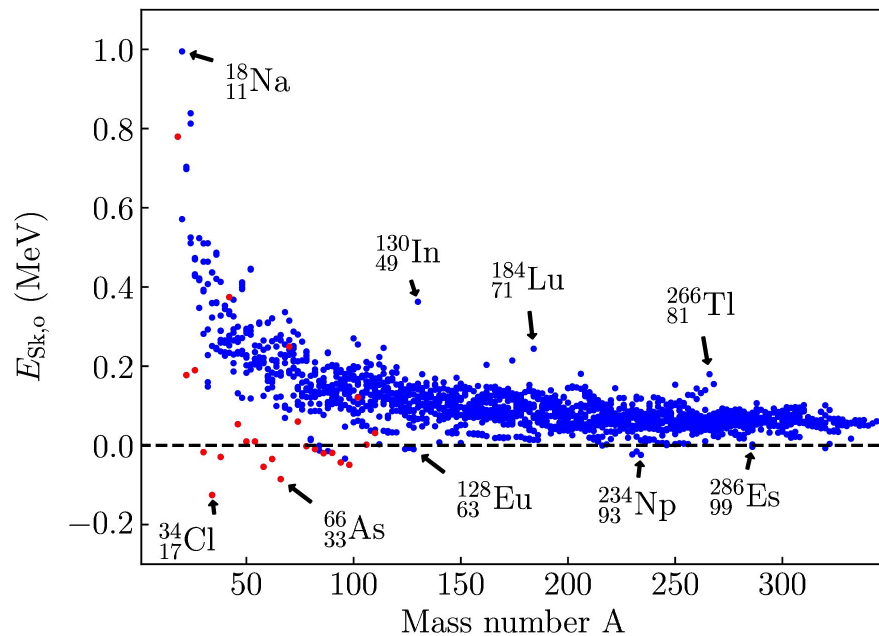


BSkG models: fission

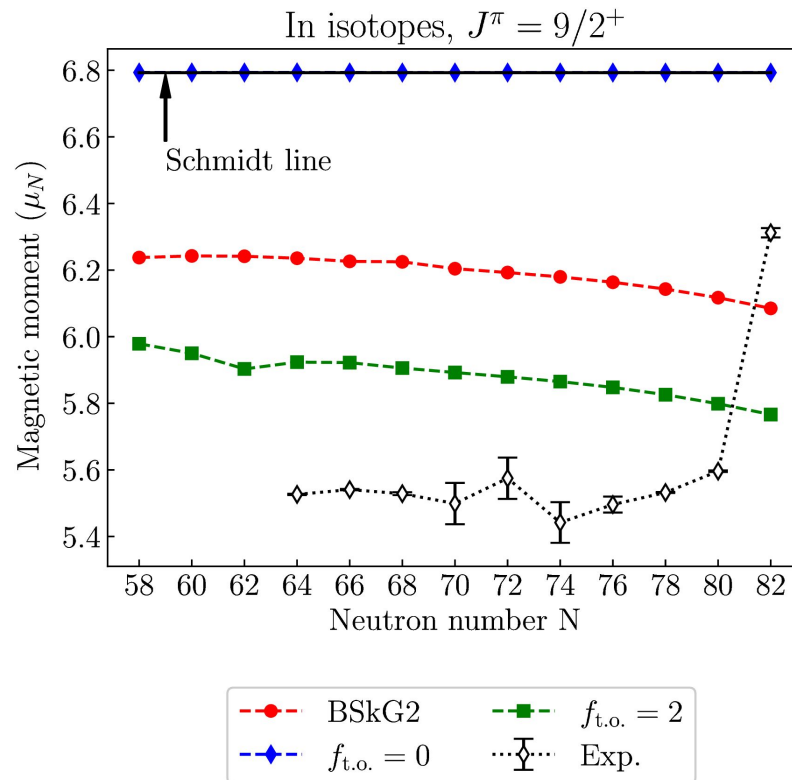
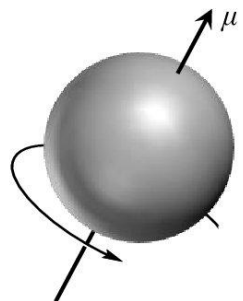


W. R. et al., in preparation.

BSkG models: time-odd energy contribution

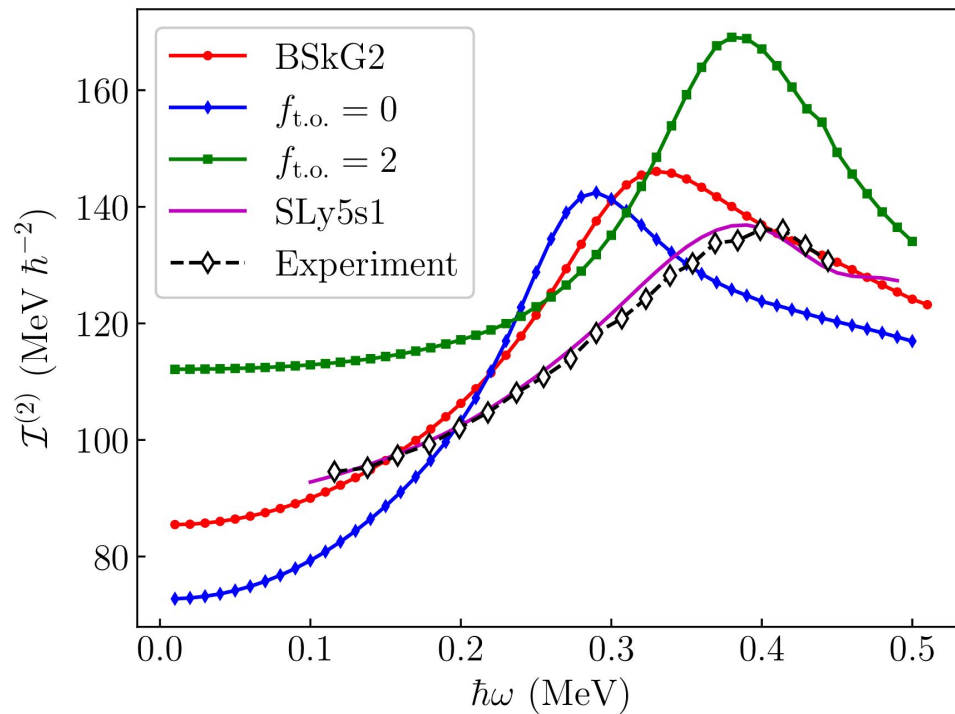
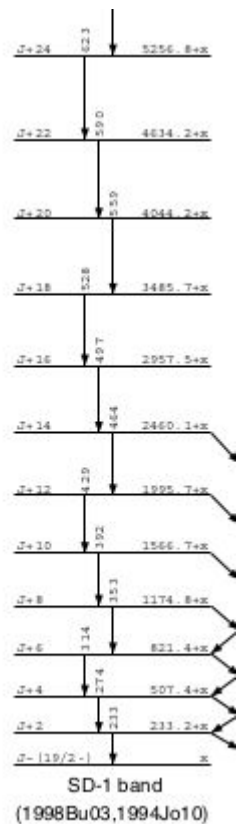


BSkG models: magnetic moments



Exp. data from A. Vernon et al., under review at Nature.
DOI:10.21203/rs.3.rs-611360/v1

BSkG models: rotational bands



Exp. data from B. Singh, Nuclear Data Sheets 97, 241 (2002).